Second harmonic of laser radiation for IR-range in mixed AgGa$_{0.6}$In$_{0.4}$Se$_2$ crystals

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ABSTRACT

In the present work, the result of investigations of the influence of different parameters on conversion efficiency in mixed AgGa$_{0.6}$In$_{0.4}$Se$_2$ crystal in conditions of existing experiments are cited. The angular dispersion coefficients for three versions of crystal AgGa$_x$In$_{1-x}$Se$_2$, differing by a content of indium, have been calculated. A comparison was made of the obtained results on conversion efficiency with analogous results in case of other crystals and with corresponding experimentally measured values. The applied analytical method makes it possible to calculate the optimum parameters of both crystal-converter and a source of radiation for conditions of uncritical phase matching in the concrete experiment.

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KEYWORDS

Second harmonic generation;
IR-range;
Mixed type crystal;
Constant-intensity approximation.

INTRODUCTION

By present, the important achievements have been attained in application of nonlinear crystals in the numerous devices of IR-range. One can note among them the prospect CdGeAs$_2$ crystals, available ZnGeP$_2$ crystals, AgGaSe$_2$ and others[1-3]. Selection of nonlinear crystals is determined by requirement of obtaining the high conversion efficiency of pump radiation in a tuning wide spectral range. As one way solving this problem, it is suggested to use chalcogenide crystals or chalcopyrite structures, for example, AgGa$_x$In$_{1-x}$Se$_2$, AgGa(Se$_{1-x}$S$_x$)$_2$[2]. In similar crystals, by changing parameter x, it is possible to realize uncritical 90^0 phase matching. This condition ensures the absence of walk-off of second harmonic energy, excluding decrease of second harmonic generation caused by birefringence.

We have chosen the perspective crystals AgGa$_x$In$_{1-x}$Se$_2$ as a subject of study among crystals of mixed type, owing to a number of its qualities. As showed in the result of experiment[4] by researchers, by choosing indium content, it is possible to perform the uncritical condition of 90^0 phase matching at second harmonic generation in near and middle IR-range. With this, a value of parameters x on wavelength of CO$_2$ laser radiation λ=9.64 mcm is equal to 0.6. The measured value of quadratic nonlinear susceptibility for AgGa$_{0.6}$In$_{0.4}$Se$_2$ crystal is equal d$_{36}$=41 pm/V[4]. For comparison, the analogous specified value for AgGaSe$_2$ crystal is equal to 39 pm/V[3,4].

For the task of application in IR range of spectrum CO$_2$ lasers that present a powerful source of optical coherent radiation in the given region of spectrum, play a leading role. If in the middle IR-region of spectrum an

efficient generation of radiation for this laser permits to realize tunable coherent radiation, then in the near IR range it can be succeeded owing to radiation of second harmonics for CO_2 laser.

To consider a wide circle of the tasks in a theory for nonlinear waves, it is necessary to solve the system of coupled nonlinear differential equations. In most cases, solution of such system in a general form is not possible, so to analyze the complete system of reduced equation, different approximation method has been used. Among them, constant-field approximation of basic radiation was widely used[5-7]. In this approximation, both the real amplitude and phase for wave are considered to be constant. The constant-field approximation depicts rightly only an initial stage of nonlinear interaction for waves until it is not generally possible to take into account the reverse influence generated or enforced waves on the intense pump wave. This leads to restricted consideration of wave interaction in real media and loss of information on features of the nonlinear process.

For analyzing of nonlinear process, it is possible to use the direct numerous of coupled equations. However, development of the analytical method will permit to receive the concrete analytical expressions and to define optimum parameters of the task for the purpose of obtaining the maximum efficiency of conversion.

To study the nonlinear optical properties of selected type of crystal, it is expedient to resort to the constant-intensity approximation[8-9], enabling to take into regard an impact of exited wave on exciting one. The given approximations permitted to consider an influence of phase effects on the process of redoubling CO_2 laser radiation frequency in these crystals of mixed type.

At the present work, cited as the result of studies for the influence of different parameters on conversion efficiency in $AgGa_{0.6}In_{0.4}Se_2$ crystal in conditions of existing experiments. These have been calculated the angular dispersion coefficients for three versions of $AgGa_xIn_{1-x}Se_2$ crystals, differing by content of indium. Comparison of received result on conversion efficiency has been made with analogous result in case of other crystals and with corresponding experimentally measured values. The ways of increasing conversion efficiency are displayed. The used analytical method permits to calculate optimum parameters of both crystal-converter and radiation source for conditions of uncritical phase match in the concrete experiment. Thus for example, we can calculate optimal crystal length at the given losses and the pump intensities, what allows one to estimate expected conversion efficiency.

THEORY

Let's analyze the process of redoubling the frequency of CO_2 laser radiation (at frequency ω_1) in $AgGa_xIn_{1-x}Se_2$ negative uniaxial crystal in case of oo→e scalar phase matching for first type.

For nonlinear conversion, theoretical analysis of wave interaction is made by using the known system of the reduced equation describing second harmonic generation (at frequency $2\omega_1$)[5-7]

$$\frac{dA_1}{dz} + \delta_1 A_1 = -i\frac{8\pi^2 d_{1eff}}{\lambda_1 n(\omega_1)} A_2 A_1^* \exp(-i\Delta z),$$

$$\frac{dA_2}{dz} + \delta_2 A_2 = -i\frac{4\pi^2 d_{2eff}}{\lambda_2 n(\omega_2)} A_1^2 \exp(i\Delta z),$$

(1)

where A_1, A_2 are complex amplitudes of pump wave and its second harmonic at frequencies $\omega_{1,2}$ ($\omega_2 = 2\omega_1$) correspondingly, k_1, k_2 are values of wave vectors for pump and second harmonic waves, $\Delta = k_2 - 2k_1$ stands for phase mismatch, $d_{1,2eff}$ are efficient nonlinear coefficient for the case îî→å scalar phase matching, $\lambda_{1,2}$ signify the wavelength of pump and second harmonic waves, $n(\omega_{1,2})$ are the indices of crystal refraction, $\delta_{1,2}$ are the coefficients of absorption for waves at frequencies of respectively.

System (1) does not include the members that are responsible for thermal effects. In the present work it is explained the investigation of frequency conversion for low value of pump intensity.

We'll solve the system with the following boundary conditions

$$A_1(z = 0) = A_{10}\exp(i\varphi_{10}), \quad A_2(z = 0) = 0, \quad (2)$$

where z=0 corresponds to the entry of crystal, and is an initial phase of pump wave at the entry of the medium.

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Solution (1) in the constant-intensity approximation which concerns the amplitude of second harmonic while considering the boundary conditions (2) at the output from crystal ($z = \ell$) leads as follows[8,9]:

$$A_2(\ell) = -i\gamma_2 A_{10}^2 \ell \ \mathrm{sinc}\lambda\ell \exp\left[2i\varphi_{10} - (\delta_2 + 2\delta_1 - i\Delta_1)\ell/2\right], \quad (3)$$

where

$$\lambda^2 = 2\Gamma^2 - (\delta_2 - 2\delta_1 + i\Delta_1)^2/4, \qquad \Gamma^2 = \gamma_1\gamma_2 I_{10},$$

$$\mathrm{sinc}x = \sin x / x, \qquad I_j = A_j A_j^*, \text{- and}$$

$$\gamma_1 = \frac{8\pi^2 d_{1eff}}{\lambda_1 n(\omega_1)}, \qquad \gamma_2 = \frac{4\pi^2 d_{2eff}}{\lambda_2 n(\omega_2)}$$

are nonlinear coefficients of waves.

From (3) it is seen that the harmonic amplitude depending on length is a periodic function. At first, at the optimal length (coherent length) transferring of basic radiation energy to the second harmonic energy happens. Then a reverse transfer of energy occurs. From (3) at $\delta_2 = 2\delta_1$ it is possible to receive optimum length of crystal. At this length in the process of frequency conversion, a harmonic signal is maximum

$$\ell_{opt} = \lambda^{-1}\arctan(\lambda/\delta_2), \text{ where } \lambda^2 = 2\Gamma^2 + \Delta^2/4.$$

Whence it appears that in this case, in contrast to the results of the constant-field approximation, a coherent length of nonlinear medium depends on pump intensity I_{10} and dissipation in a medium. By increasing in pump intensity and mismatch, the optimum length decreases. When we ignore the losses

$$\ell_{opt} = 0.5\pi / (2\Gamma^2 + \Delta^2/4)^{1/2} \ [8,9].$$

At $\gamma_1 = 0$ and $\delta_j = 0$ from (3) we have an expression for conversion efficiency in the constant-field approximation.

From (3) it is possible to obtain the analytical expression for conversion efficiency of pump radiation to second harmonic $\eta_2(\ell) = I_2(\ell)/I_{10}$.

$$\eta_2(\ell) = \gamma_2^2 I_{10}\ell^2 \ \mathrm{sinc}^2\lambda\ \ell \ \exp\left[-(\delta_2 + 2\delta_1)\ell\right]. \quad (4)$$

An important requirement for the efficient proceeding nonlinear optical process is the necessity of fulfillment of optimum phase correlation between interacting waves. The violation of this condition leads to mismatch of waves phase and, as a consequence, to decrease of conversion frequency efficiency. One of the basic reasons that cause for break of condition of optimum phase correlation is the phase mismatch. At frequency conversion in the conditions of phase mismatch, it is impossible to fulfill the complete transfer of basic radiation energy to second harmonic energy. In this case the spatial beatings of harmonic amplitudes are observed. This time, the minimums of harmonic intensity beatings, as an analysis shows in the constant-intensity approximation, depend on nonlinear susceptibilities of crystal[11]. This fact permits to define the nonlinear susceptibilities of substances by a simple way, more precise than in the constant-field approximation. With an increase in phase mismatch, spatial frequency increases, but at this time, maximum value of second harmonic intensity decreases.

In the experiment for real frequency converters, it is impossible to ensure a condition of phase agreement, i.e. phase matching ($\Delta=0$). An error in following the condition of phase matching determines the width of phase matching. Spectral width of pump radiation line, deviation from phase matching angle due to divergence of laser radiation, and instability of temperature for a crystal converter, all contribute to mismatch. Hence receiving information, in particular, on angular width of phase matching, will permit to calculate the maximum divergence of light beam for pumping. As well, determination of conditions for realizing uncritical phase matching at chosen length of pump wave is important for exclusion of taking down the influence of birefringent walk-off on generation efficiency. This fact allows one to take away the restriction of length of the used crystals[4,7,12].

Let's define an angular width of phase matching in uniaxial crystal for mixed type AgGa$_x$In$_{1-x}$Se$_2$ in case of second harmonic generation of CO$_2$ laser radiation on three wavelength of pump: 9.64 mcm, 9.55 mcm and 9.31 mcm (scalar phase matching of the first type for ○○→e interaction). We'll carry out the calculation of deviation angle from the direction of phase matching according to[7] for three values reflecting indium content in crystal (0, 0.3 and 0.4). With this, there were used Sellmeier coefficients cited in[4,10].

The results of calculations are presented for angular dispersion coefficient of the first and second orders

TABLE

Crystal	λ, mcm	n_o^{ω}	n_e^{ω}	$n_o^{2\omega}$	$n_e^{2\omega}$	d_{36}, pm/V	Phase matching type	ϑ_s, degree	angular dispersion coefficient of first order, cm$^{-1}\cdot$ang. min.$^{-1}$
AgGaSe$_2$	9.31	2.597798	2.565611	2.616307	2.58463	39.0[12]	oo→e	47.9[4]47.9672	0.048353
AgGaSe$_2$	9.55	2.596647	2.563607	2.616158	2.584178	39.0[12]	oo→e	49.1[4]49.1893	0.047611
AgGaSe$_2$	9.64	2.5965652.596[4]	2.563902	2.615704	2.584012.583[2]	39.0[12]	oo→e	49.6[4]49.6679	0.046432
AgGa$_{0.7}$In$_{0.3}$Se$_2$	9.31	2.606749	2.584379	2.624120	2.602546	40.6[4]	oo→e	63,5[4]	0.026456
AgGa$_{0.7}$In$_{0.3}$Se$_2$	9.55	2.583259	2.605674	2.623659	2.602059	40.6[4]	oo→e	65.0[4]	0.024782
AgGa$_{0.7}$In$_{0.3}$Se$_2$	9.64	2.605264	2.582832	2.623489	2.60188	40,6[4]	oo→e	66.0[4]	0,023831
AgGa$_{0.6}$In$_{0.4}$Se$_2$	9.31	2.609726	2.590959	2.626858	2.608989	41.0 [13]	oo→e	77.6[4]	0.011648
AgGa$_{0.6}$In$_{0.4}$Se$_2$	9.55	2.609726	2.589858	2.626432	2.608496	41.0 [13]	oo→e	83.4[4]	0.006216
									angular dispersion coefficient of second order, cm$^{-1}\cdot$ang. min.
AgGa$_{0.6}$In$_{0.4}$Se$_2$	9.64	2.6082772.6081[4]	2.589438	2.626222	2.608315	41.0 [13]	oo→e	90.0[4]	0.0000194

in the TABLE.

RESULTS AND DISCUSSION

To study the ways of increasing frequency conversion efficiency in AgGa$_x$In$_{1-x}$Se$_2$ crystal of CO$_2$ laser radiation in IR range, we'll make the numerous calculation of the analytical expression for conversion efficiency (4), received in the constant- intensity approximation, the parameters of the task are chosen according to conditions of existing experiments for the given crystal[4,14]. In Figures. 1-3 the dynamic process of frequency conversion is shown to the second harmonic in AgGa$_{0.6}$In$_{0.4}$Se$_2$ crystal.

In Figure 1, the dependencies of frequency conversion efficiency on length of crystal $\eta_2(\ell)$ are presented. These are considered as 3 version of conversion differed by CO$_2$ laser pump intensities, radiating at wavelength in 9.55 mcm. From the behavior of curves differing by monotonous behavior in case of the constant-field approximation, it follows that there exists an optimum value of crystal length at which conversion efficiency is maximum. As far as pump intensity grows the maximum of conversion is reached at lower lengths of a crystal, i.e. by increasing the pump intensity, the coherent length of crystal decreases.

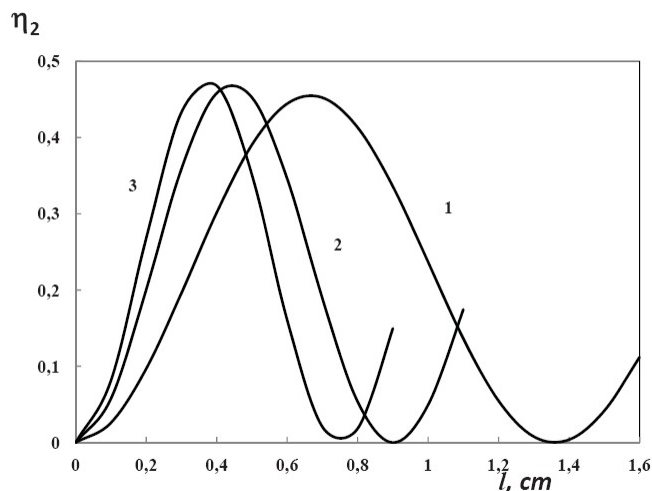In Figure 2, the dependencies on pump intensity for three lengths of crystals are cited. As is seen in fig-

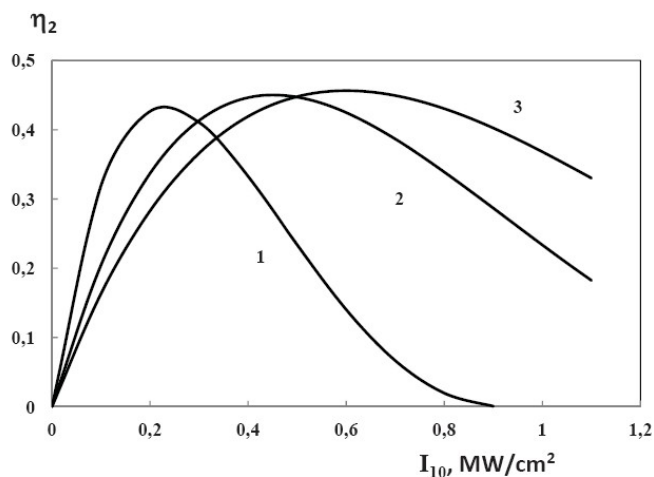**Figure 1: Dependences of conversion efficiency of radiation energy of pump wave (λ=9.55 mcm) to energy of wave of second harmonic η_2 on lengths of AgGa$_{0.6}$In$_{0.4}$Se$_2$ crystal l calculated in the constant-intensity approximation for δ_1=0.06 cm^{-1}, δ_2=0.08 cm^{-1} [4], Δ=0.06 cm^{-1} at pump intensity of I$_{10}$= 0.55 MW/cm² (curve 1), 1.25 MW/cm² (curve 2) and 1.8 MW/cm² (curve 3).**

ure, CO$_2$ laser radiation, generating at wavelength in 9.55 mcm, maximum efficiency is converted to second harmonic wave at optimum value of pump intensity. From comparison of curves 1, 2 and 3 it is seen that optimum value of pump intensity falls down as crystal length increase. It is explained by the fact that at greater values of pump intensity the coherent length of crystal, where maximum conversion occurs, comes out at lower geometric dimension of crystal-converters.

As is known in the mixed structures AgGa$_x$In$_{1-x}$Se$_2$

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Figure 2 : Dependences of conversion efficiency of radiation energy of pump wave (λ=9.55 mcm) to energy of wave of second harmonic in AgGa$_{0.6}$In$_{0.4}$Se$_2$ crystal η_2 as a function of the pump intensity calculated in the constant-intensity approximation for δ_1=0.06 cm^{-1}, δ_2=0.08 cm^{-1} [4], Δ=0.06 cm^{-1} at crystal length of l= 1.05 cm [4], (curve 1), 0.75 cm (curve 2) and 0.65 cm (curve 3).

crystal properties undergo the influence of indium content[4]. In Figure 3 the results of the analysis for frequency conversion process are represented in case of 3 different concentration of indium in crystal: 0, 0.3 and 0.4. There are considered three versions of CO$_2$ laser wavelengths: 9.31 mcm, 9.55 mcm and 9.64 mcm. The groups 1 and 4 (containing on three curves everyone) correspond to dependencies of $\eta_2(\vartheta)$ in case of three wavelengths of pump radiation at lengths of AgGa$_{0.7}$In$_{0.3}$Se$_2$ crystal (x=0.7) equal to 1.05cm and 0.65 cm respectively. The groups 2 and 5 (containing on three curves everyone) correspond to dependencies of $\eta_2(\vartheta)$ to three wavelengths of pump radiation at crystal lengths AgGa$_{0.6}$In$_{0.4}$Se$_2$ (x=0.6), equal to 1.05 cm and 0.65 cm. The group 3 (containing on three curves) corresponds to dependencies in case of 3 wavelengths of pump radiation at length of AgGaSe$_2$ crystal (x=1) equal to 0.8 cm. In each group, the upper curve corresponds to wavelength of radiation equal to 9.64 mcm, the middle one corresponds to 9.55 mcm, and lower curve corresponds to 9.31 mcm.

By comparing the behavior of curves 3, 4 and 5, it is seen that with increasing the concentration of indium in the mixed crystal from 1 to 0.6, the dependence $\eta_2(\vartheta)$ becomes more flat. It testifies the transition to the regime of uncritical character of crystal towards fol-
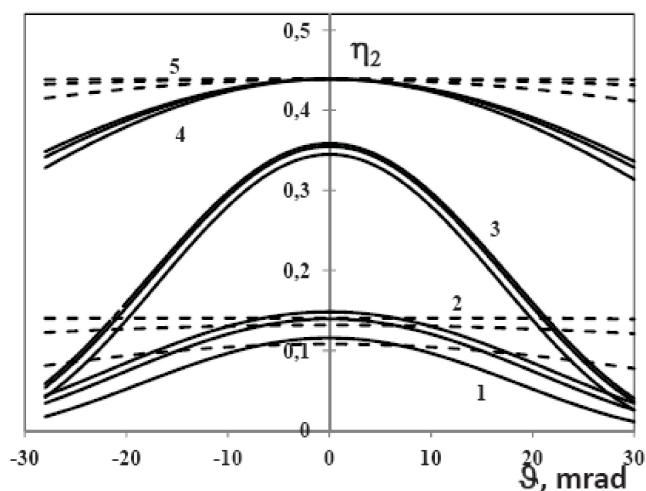

Figure 3 : Dependences of conversion efficiency of radiation energy of pump wave to energy of wave of second harmonic in AgGa$_x$In$_{1-x}$Se$_2$ crystal η_2 as a function of the phase mismatch calculated in the constant-intensity approximation at pump intensity of I$_{10}$= 0.6 MW/cm^2 for x=0.7 - AgGa$_{0.7}$In$_{0.3}$Se$_2$ (groups of curves 1 and 4), 0.6 - AgGa$_{0.6}$In$_{0.4}$Se$_2$ (groups of dashed curves 2 and 5), 1 - AgGaSe$_2$ (group of curves 3). In each group, the upper curve corresponds to wavelength of radiation equal to 9.64 mcm, the middle one corresponds to 9.55 mcm, and lower curve corresponds to 9.31 mcm. Here crystal length of l = 1.05 cm [4], (groups of curves 1 and 2), 0.8 cm [4] (group of curves 3) and 0.65 cm (groups of curves 4 and 5). For AgGaSe$_2$ crystal δ_1=0.09 cm^{-1}, δ_2=0.15 cm^{-1} [4] and AgGa$_x$In$_{1-x}$Se$_2$ δ_1=0.06 cm^{-1}, δ_2=0.08 cm^{-1} [4].

lowing condition of phase matching, thus for instance, in AgGaSe$_2$ crystal the change of conversation efficiency by 0.036 % takes place in the angular range of changes from -0.6 mrad to +0.6 mrad. By substituting some part of Ga for indium to content x=0.7 (AgGa$_{0.7}$In$_{0.3}$Se$_2$) in a crystal leads to the analogous change of efficiency, but already in the angular range greater 1.67 times (from -1 mrad to +1 mrad). The further replacement of indium to crystal to x=0.6 (i.e. AgGa$_{0.6}$In$_{0.4}$Se$_2$) increases angular range 33 times (-20 mrad to +20 mrad) in comparison with a case of AgGaSe$_2$ crystal. Hence, in AgGa$_{0.6}$In$_{0.4}$Se$_2$ crystal, uncritical behavior towards following phase matching condition is observed in angular range greater that in AgGa$_{0.7}$In$_{0.3}$Se$_2$ and in AgGaSe$_2$. This question was studied experimentally, in[4], but at the length of experimental sample for AgGa$_x$In$_{1-x}$Se$_2$ crystal equal to 1.05 cm. In our case, it corresponds to curves group 1 (x=0.7) and group 2 (x=0.6). By comparing the curves in group 1 and 4, and those of groups 2 and 5, we see that the use of optimum length of a crystal-converter may enable to increase the conver-

sion efficiency three times from $\eta_2 = 0.15$ to 0.45.

As well, it is seen in Figure 3 that in conditions of a real experiment, the maximum expected conversion efficiency in case of $AgGa_{0.6}In_{0.4}Se_2$ crystal is more than conversion efficiency in $AgGaSe_2$ crystal in 1.225 times and only on 0.0378 % conversion efficiency in $AgGa_{0.6}In_{0.4}Se_2$ is more than in $AgGa_{0.7}In_{0.3}Se_2$ crystal.

Thus, theoretical investigation of frequency conversion in mixed crystals with regard for phase effects enables to find out the ways of increasing conversion efficiency. And namely at the given value of crystal converter length it is possible to calculate the optimum value of pump intensity, as well as to calculate the coherent length of crystal-converter at chosen pump intensity of laser radiation. The analytical method also permits to estimate an expected conversion efficiency at different wavelengths of leaser radiation. There has been estimated the angular width of phase matching at different concentrations of indium for crystals of mixed type. The conditions promoting a mode of uncritically to performance of a condition of phase synchronism were revealed.

CONCLUSION

The results of the studies carried out will permit to elaborate the reliable highly efficient generators of second harmonic in CO_2 lasers. The method of analysis for second harmonic generation in $AgGa_{0.6}In_{0.4}Se_2$ crystals developed in the present work may be used for considering the process of frequency conversion in other perspective crystals of IR range, as well for examination of nonlinear optical waves in similar crystals.

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