



July 2007

Volume 2 Issue 1

# CHEMICAL TECHNOLOGY

*An Indian Journal*

Trade Science Inc.

*Full Paper*

CTAIJ 2(1) 2007 [13-23]

## Desorption Of Carbon Dioxide From Promoted Hot Potassium Carbonate In An Industrial Stripper Using Penetration Theory

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*Received: 26<sup>th</sup> March, 2007*

*Accepted: 31<sup>st</sup> March, 2007*

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### ABSTRACT

A mathematical model was used for simulation of CO<sub>2</sub> desorption from promoted hot potassium carbonate solution. The combined effects of chemical reaction and mass transfer were conveniently and adequately treated within the framework of the penetration-surface renewal theory. The vapor-liquid equilibrium data for the un-promoted carbonate-CO<sub>2</sub> was employed for developing the model which seems to be adequate at low concentration of amine for the system. The operating data for carbon dioxide desorption from DEA-hot potassium carbonate solution in an industrial stripper has been compared to model predictions. The process model was used to predict profiles of different dependent parameters in a commercial desorption unit. The effects of the promoter concentration, the promoter type and the inlet temperature of rich solution on the performance of an industrial regeneration unit have also been examined. It was found that the inlet liquid temperature impact upon both the mass transfer and the reboiler steam consumption rate. © 2007 Trade Science Inc. - INDIA

### KEYWORDS

Hot potassium carbonate;  
Stripper;  
Carbon dioxide desorption;  
Promoters;  
Penetration theory;  
Enhancement factor;  
Regeneration.

### INTRODUCTION

For economic reasons it is almost necessary to regenerate the spent solution from a carbon dioxide absorption column so that the absorbent can be recycled. The design of columns for stripping solutions which contain physically dissolved gases is comparatively simple. However, complications arise

when chemical reactions are involved. The relevant information on this subject in the literature is very scarce, although the investment for the desorption columns with or without chemical reactions is considerably greater than that for the absorption columns.

The regeneration often uses steam or heated inert gas as stripping agents. As a result, an accurate

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design based on proper chemical and mass transfer data could lead to significant energy savings. The gas to be purified is generally under pressure; therefore absorber operates under high pressure, while stripper operates at about atmospheric pressure. Essentially, the process depends on the pressure difference between the absorber and stripper and a substantial difference in temperature is not necessary. In stripping columns, steam (either live or from a reboiler at the bottom of stripper) or hot air are used to strip the carbon dioxide from absorbent. The quantity of stripping vapor required depends upon the solution purity needed to produce the required product gas, the stripping column height and the nature of the solution.

The applicability of potassium carbonate to  $\text{CO}_2$  removal has been known for many years. A German patent granted as early as 1908, described a process for absorbing  $\text{CO}_2$  in a hot solution of potassium carbonate and then stripping the solution by pressure reduction without additional heating<sup>[1]</sup>. In 1924, Williamson and Mathews studied the rate of absorption of  $\text{CO}_2$  in potassium carbonate solution and found that increasing temperature greatly increased the rate of absorption<sup>[2]</sup>. The hot carbonated process was developed by Benson et al.<sup>[3, 4]</sup>. Benson indicated that because the  $\text{CO}_2$  concentration in solution decreases rapidly with decreased partial pressure of  $\text{CO}_2$  over it, solution regeneration can be carried out most effectively at a very low pressure<sup>[5]</sup>. The high temperature increases the solubility of potassium bicarbonate thus permitting operation with a highly concentrated solution that increases the carrying capacity for acid gases per gallon of solution. In addition steam required to heat the solution for stripping temperature is less. The basic hot carbonated process has since undergone several improvements<sup>[6, 7]</sup>, that some of these aimed primarily at greater heat economy<sup>[8, 9, 10]</sup>.

The concept of adding amine to carbonate systems for enhancement of  $\text{CO}_2$  absorption has been known for a long time<sup>[11-16]</sup>. However, there is no information available in the literature regarding the desorption of carbon dioxide from potassium carbonate in an industrial regeneration column. Therefore, we decided to study the phenomenon of desqure research including the effect of parameters such as promoter type and concentration which are

discussed in the present work. Other areas include the effect of amine additives on the equilibrium and the influence of reactants and products diffusion in the mass transfer boundary layer on the enhancement factor.

In our previous work we have investigated the absorption of carbon dioxide into potassium carbonate in an absorption column<sup>[17]</sup>, while in this work desorption of carbon dioxide from potassium carbonate in a stripper column is investigated. A general model for the mass transfer/ reaction processes in carbon dioxide stripper using promoted hot potassium carbonate has been developed and the combined effects of mass transfer and chemical reaction was treated by the surface-renewal penetration theory. In addition, the effect of various parameters on the performance of an industrial stripper has been investigated.

### Process setup

Figure 1 shows a schematic diagram of a conventional split-flow absorber-stripper<sup>[18]</sup>. The system consists of two columns, the absorber and the stripper (or regenerator) where both columns are packed bed type. The feed gas enters the absorber, which operates at an elevated pressure, and is contacted counter-currently with the lean liquid from the regenerator, and essentially all of the carbon dioxide is removed. The rich liquid loaded with carbon dioxide from the bottom of the absorber is first flashed nearly to 1.15 atm in a throttling valve and subsequently passes through the stripper where it is stripped counter-currently by the stream generated by boiling solution in the bottom of the stripper. As the solution flows downward through the regenerator in the counter-current mode with steam,  $\text{CO}_2$  is stripped from the solution. A portion of the lean solution from the regenerator is cooled and fed into

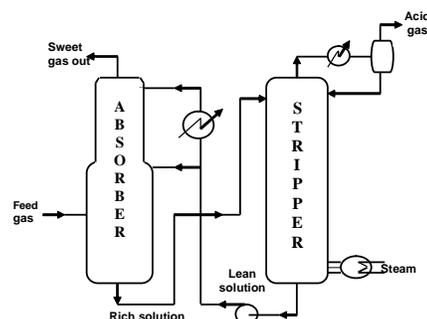


Figure 1: Schematic diagram of a conventional split-flow absorber-stripper arrangement

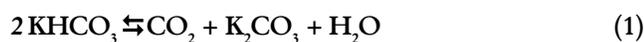
TABLE 1: Characteristics of the stripping tower, packing, reboiler and system for CO<sub>2</sub> desorption<sup>[18]</sup>.

Parameters	Value	units
Height of packing	26	m
Diameter of packed bed	5.5	m
Packing size (d <sub>p</sub> )	40	mm
Packing shape	metal mini rings	-
Specific surface of packing (a)	123	mm <sup>-1</sup>
Packing void fraction	0.975	-
Reboiler heat load	15.60×10 <sup>7</sup>	kJh <sup>-1</sup>
Boiling point of solution in reboiler	401	K
Stripper pressure	1.15	atm

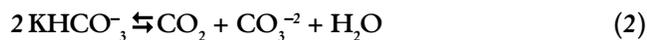
the top of the absorber while the major portion is added at a point below the top without any change in temperature. This simple modification, which is called split-flow process, raises the temperature of the rich liquid and lowers the amount of heat needed for heating the solution to the regeneration temperature. The acid gases together with some water vapor pass overhead from the stripper and through a condenser. TABLE 1 shows the characteristics and specification of a typical industrial stripping column and reboiler<sup>[18]</sup>.

### Chemical reactions

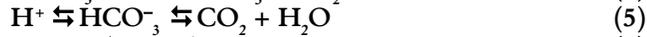
The basic reaction chemistry for decomposition of KHCO<sub>3</sub> is represented by the following reversible reaction<sup>[19,20]</sup>:



Since potassium carbonate and bicarbonate are both strong electrolytes, it may be assumed that the metal is present only in the form of K<sup>+</sup> ions, so reaction (1) may be more realistically represented in the ionic terms as:



The above reaction is evidently made up of a sequence of elementary steps<sup>[19]</sup>:



Reactions (4) through (7) are fast while reaction (3) is slow and, hence, the rate controlling step, with the following rate equation<sup>[14, 19, 21]</sup>:

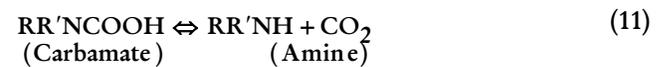
$$r_{\text{OH}} = k_{\text{OH}}[\text{OH}^-][\text{CO}_2]_e - [\text{CO}_2] \quad (8)$$

where  $K_{\text{OH}}$  is the backward rate constant and  $[\text{CO}_2]_e$  is the equilibrium concentration of CO<sub>2</sub>. Carbonate-bicarbonate system is a buffer solution, thus the concentration of the OH<sup>-</sup> ion in the solution near the surface of the liquid is not significantly depleted by the absorbed CO<sub>2</sub>. In this case, the carbon dioxide undergoes a pseudo-first order reaction and Eq. (8) may be rewritten as<sup>[14, 16, 21]</sup>:

$$r_{\text{OH}} = k_1([\text{CO}_2]_e - [\text{CO}_2]) \quad (9)$$

Where  $k_1$  denotes an apparent first-order rate constant.

When a small amount of amine is added into the solution, the desorption rate of carbon dioxide is enhanced greatly according to the following reactions<sup>[14]</sup>:



At higher temperatures industrial operating conditions, the rate of reaction (11) increases significantly. As such, the system is better represented by the homogeneous catalysis mechanism<sup>[14, 20-23]</sup> and, hence, reaction (10) becomes the rate-controlling step. Using this approach in deriving Eq. (9) results in the following pseudo-first order rate equation for  $r_{\text{AM}}$ <sup>[21]</sup>:

Where  $k_2$  is an apparent first-order rate constant.

Adding Eqs. (9) and (12) leads to the overall pseudo-first order rate equation for carbon dioxide with promoted hot potassium carbonate in liquid phase:

$$r_{\text{AM}} = k_{\text{AM}}[\text{Am}][\text{CO}_2]_e - [\text{CO}_2] = k_2([\text{CO}_2]_e - [\text{CO}_2]) \quad (12)$$

Where  $k_2$  is an apparent first-order rate constant.

Adding Eqs. (9) and (12) leads to the overall pseudo-first order rate equation for carbon dioxide with promoted hot potassium carbonate in liquid phase:

$$r = (k_{\text{OH}}[\text{OH}^-] + k_{\text{AM}}[\text{Am}])([\text{CO}_2]_e - [\text{CO}_2]) \quad (13)$$

$$= k([\text{CO}_2]_e - [\text{CO}_2])$$

Where  $k$  is the overall apparent first-order rate constant and defined as:

$$k = (k_{\text{OH}}[\text{OH}^-] + k_{\text{AM}}[\text{Am}]) \quad (14)$$

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The governing equations of the model for a packed stripper<sup>[24]</sup> can be derived by carrying out the material and energy balance around a differential height of the column shown in Figure 2. The envelope III is an elemental volume in the differential packed height ( $\Delta h$ ) of the stripper, consisting of the gas and liquid phases denoted by envelopes I and II, respectively. In developing the model equations we assume steady-state conditions and negligible pressure drop along the bed. It is also assumed that  $\text{CO}_2$  and  $\text{H}_2\text{O}$  are the only components transported across the interface and the reboiler in the stripper can be modeled as a well-mixed equilibrium stage.

### Mass balance

#### 1. Gas phase

A differential mole balance in the gas phase around ( $dh$ ) provides a differential equation for the gas flow along the bed:

$$\frac{dG}{dh} = (N_{\text{CO}_2} - N_{\text{H}_2\text{O}})a \quad (15)$$

Where  $G$  is superficial molar velocity of gas,  $N_{\text{CO}_2}$  and  $N_{\text{H}_2\text{O}}$  are mass transfer fluxes of  $\text{CO}_2$  and  $\text{H}_2\text{O}$ , and  $a$  is the specific surface area of packing.

A differential mole balance in the gas phases for  $\text{CO}_2$  and  $\text{H}_2\text{O}$  also gives the following differential equations for mole fraction of carbon dioxide and water in the gas phase:

$$\frac{dy_{\text{CO}_2}}{dh} = \frac{(N_{\text{H}_2\text{O}}y_{\text{CO}_2} + N_{\text{CO}_2}(1 - y_{\text{CO}_2}))a}{G} \quad (16)$$

$$\frac{dy_{\text{H}_2\text{O}}}{dh} = \frac{-(N_{\text{CO}_2}y_{\text{H}_2\text{O}} + N_{\text{H}_2\text{O}}(1 - y_{\text{H}_2\text{O}}))a}{G} \quad (17)$$

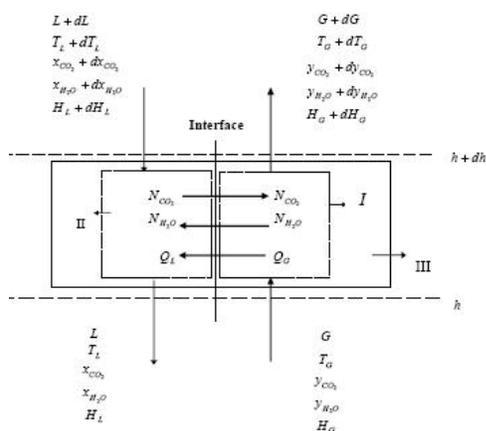


Figure 2: Differential section of packed stripper

#### 2. Liquid phase

Here it has been assumed that for the amine-promoted carbonate solution the reaction is fast and hence the reaction take place at the same rate at which the carbon dioxide is desorbed<sup>[20, 21, 23]</sup>. A differential mole balance in the liquid phase results in:

$$\frac{dL}{dh} = -N_{\text{H}_2\text{O}} a \quad (18)$$

where  $L$  is the superficial molar velocity of the liquid. In derivation of Eq. (18) the  $\text{CO}_2$  generated by reaction (1) is assumed to be desorbed from the liquid phase, so that the reaction (1) has no effect on the change of liquid molar flow rate.

The differential moles balance for  $\text{K}_2\text{CO}_3$  in the liquid phase gives:

$$\frac{d(Lx_{\text{K}_2\text{CO}_3})}{dh} = -N_{\text{CO}_2} a \quad (19)$$

Replacing  $dL$  by Eq. (18) gives rise to the equation for mole fraction of  $\text{K}_2\text{CO}_3$ :

$$\frac{dx_{\text{K}_2\text{CO}_3}}{dh} = \frac{(N_{\text{H}_2\text{O}}x_{\text{K}_2\text{CO}_3} - N_{\text{CO}_2})a}{L} \quad (20)$$

Mole balances for  $\text{KHCO}_3$  and  $\text{H}_2\text{O}$  also yield the following equation in the liquid phase:

$$\frac{dx_{\text{KHCO}_3}}{dh} = \frac{(N_{\text{H}_2\text{O}}x_{\text{KHCO}_3} + 2N_{\text{CO}_2})a}{L} \quad (21)$$

$$\frac{dx_{\text{H}_2\text{O}}}{dh} = \frac{-(N_{\text{H}_2\text{O}}(1 - x_{\text{H}_2\text{O}}) + N_{\text{CO}_2})a}{L} \quad (22)$$

#### Concentration of ions and free $\text{CO}_2$

In the present study, the concentration of hydroxyl, carbonate, bicarbonate ions, and free  $\text{CO}_2$  are obtained by chemical equilibrium and charge balance<sup>[15, 16, 23, 26]</sup>. The parameter which is usually employed to describe the liquid-phase composition is the fractional saturation defined as<sup>[22]</sup>:

$$\alpha = \frac{[\text{HCO}_3^-]}{[\text{K}^+]} = \frac{[\text{HCO}_3^-]}{2m} \quad (23)$$

where  $m$  is the molarity of the solution (i.e. the total  $\text{K}_2\text{CO}_3$  concentration<sup>[16, 25-27]</sup>).

The law of electrical neutrality suggests that:

$$2[\text{CO}_3^{2-}] + [\text{HCO}_3^-] = [\text{K}^+] \quad (24)$$

Replacing  $[\text{HCO}_3^-]$  by Eq. (23) give rise to the following equation for concentration of carbonate ion<sup>[22,27]</sup>:  $[\text{HCO}_3^-]$

$$[\text{CO}_3^{2-}] = m(1-\alpha) \quad (25)$$

In a carbonate-bicarbonate mixture the concentration of hydroxyl ion depends on the ratio of carbonate to bicarbonate and is given by the following expression<sup>[16,25,28]</sup>:

$$[\text{OH}^-] = \frac{K_w [\text{CO}_3^{2-}]}{K_6 [\text{HCO}_3^-]} \quad (26)$$

Where  $K_w$  is the stoichiometric equilibrium constant of water and  $K_6$  is the second dissociation constant for carbonic acid in reaction (6).

Substituting Eqs. (23) and (25) into Eq. (26) give rise to the following equation for the concentration of hydroxyl ion as a simple function of  $\alpha$ <sup>[26]</sup>:

$$[\text{OH}^-] = \frac{K_w}{K_6} \frac{1-\alpha}{2\alpha} \quad (27)$$

According to Eqs. (5), (6), (23) and (25), the equilibrium concentration of free  $\text{CO}_2$  in liquid is given by<sup>[16,22,23,25]</sup>:

$$[\text{CO}_2]_e = 4m \frac{K_6}{K_5} \frac{\alpha^2}{1-\alpha} \quad (28)$$

Where  $K_5$  is the first dissociation constant for carbonic acid in reaction (5).

Since potassium carbonate and bicarbonate are both strong electrolytes, combining Eqs. (23) and (24), results in the following relationship for  $\alpha$ :

$$\alpha = \frac{x_{\text{KHCO}_3}}{x_{\text{KHCO}_3} + 2x_{\text{K}_2\text{CO}_3}} \quad (29)$$

where  $x_{\text{K}_2\text{CO}_3}$  and  $x_{\text{KHCO}_3}$  are mole fractions of potassium carbonate and bicarbonate, respectively.

### Energy balance

A differential energy balance for the gas and liquid phases around the differential height (dh), gives rise to the following differential equations for the temperatures of the gas and liquid phases:

$$\frac{dT_g}{dh} = \frac{(N_{\text{H}_2\text{O}} - N_{\text{CO}_2})aT_g}{G} + \frac{(N_{\text{CO}_2}C_{\text{PCO}_2}T_L - N_{\text{H}_2\text{O}}C_{\text{PH}_2\text{O}}T_g)a}{GG_G} - \frac{h_g a (T_g - T_L)}{GG_G} \quad (30)$$

$$\frac{dT_L}{dh} = \frac{N_{\text{H}_2\text{O}} a T_L}{L} + \frac{(N_{\text{CO}_2} C_{\text{PCO}_2} T_L - N_{\text{H}_2\text{O}} C_{\text{PH}_2\text{O}} T_g) a}{LC_{\text{PL}}} - \frac{h_g a (T_g - T_L)}{GC_{\text{PG}}} + \frac{(N_{\text{CO}_2} \Delta \text{CO}_2 - N_{\text{H}_2\text{O}} \Delta \text{H}_2\text{O}) a}{LC_{\text{PL}}} \quad (31)$$

### Reboiler

Heat is supplied to the column by steam coils installed in the reboiler. Since the amount of heat needed to rise the temperature of the solution leaving the reboiler is insignificant, all of the thermal energy is consumed to evaporate water which leaves the reboiler as vapor<sup>[20]</sup>. Hence:

$$G_R = \frac{Q_R}{H_{\text{Vapor}}} \quad (32)$$

where  $Q_R$  is molar flow rate of water vapor leaving the reboiler,  $Q_R$  the amount of heat which is supplied by condensation of steam in the steam coils, and  $H_{\text{Vapor}}$  the enthalpy of superheated steam leaving the reboiler given by<sup>[29,31]</sup>:

$$H_{\text{Vapor}} = \Delta H_{\text{H}_2\text{O}}|_{T_{\text{ref}}} + C_{\text{P}_{\text{vapor}}} (T_R - T_{\text{ref}}) \quad (33)$$

in which,  $H_{\text{ref}}$  is the heat of vaporization of water at  $T_{\text{ref}}$ ,  $C_{\text{P}_{\text{VAPOR}}}$  the molar specific heat of vapor, and  $T_R$  the boiling point of solution in reboiler.

### Mass transfer

In this work the combined effect of mass transfer and chemical reaction is treated by Danckwerts's surface-renewal penetration theory.

According to this model the rate of mass transfer of  $\text{CO}_2$  in the liquid phase<sup>[23,28]</sup> is governed by:

$$N_{\text{CO}_2} = E k_L (C_{\text{CO}_2e} - C_{\text{CO}_2i}) \quad (34)$$

where  $C_{\text{CO}_2i}$  is the concentration of carbon dioxide at the interface,  $C_{\text{CO}_2e}$  the equilibrium concentration of un-reacted carbon dioxide in the bulk of liquid,  $k_L$  the physical mass transfer coefficient, and  $E$  the enhancement factor defined as the ratio of the rate of desorption of  $\text{CO}_2$  in the presence of chemical reaction to that obtained from physical desorption<sup>[23,25,27]</sup>:

$$E = \sqrt{1 + \frac{D_{\text{LCO}_2} k_{\text{OH}} [\text{OH}^-] + D_{\text{LCO}_2} k_{\text{Am}} [\text{Am}]}{k_L^2}} \quad (35)$$

The rate of mass transfer of carbon dioxide in

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the gas phase is as follows:

$$N_{\text{CO}_2} = k_{g,\text{CO}_2} (P_{\text{CO}_2,i} - P_{\text{CO}_2}) \quad (36)$$

where  $K_{g,\text{CO}_2}$  is gas phase mass transfer coefficient of carbon dioxide. Eq. (36) can be rewritten in terms of the physical solubility of  $\text{CO}_2$  in the reactive  $\text{K}_2\text{CO}_3$  solution as:

$$N_{\text{CO}_2} = \frac{k_{g,\text{CO}_2}}{H} (C_{\text{CO}_2,i} - C_{\text{CO}_2}) \quad (37)$$

Using both gas and liquid side resistances, and combining Eqs. (34) and (37) followed by eliminating the interface partial pressure of  $\text{CO}_2$ , one can reach to the following equation for the desorption rate [23,27]:

$$N_{\text{CO}_2} = \frac{k_{g,\text{CO}_2} k_L E}{k_{g,\text{CO}_2} + k_L E H} = K_{L,\text{CO}_2} (C_{\text{CO}_2,e} - C_{\text{CO}_2}) \quad (38)$$

where  $K_{L,\text{CO}_2}$  is overall liquid phase mass transfer coefficient of carbon dioxide [25,30].

Because vapor is a saturated steam and the temperature of vapor is more than the temperature of liquid at all points, steam is condensed to liquid phase across the interface. Therefore the mass transfer rate of water per unit interfacial area is:

$$N_{\text{H}_2\text{O}} = \frac{h_c \Delta T}{\Delta H_{\text{H}_2\text{O}}} \quad (39)$$

where  $h_c$  is condensation heat-transfer coefficient [32],  $\Delta H_{\text{H}_2\text{O}}$  heat of vaporization of water, and  $\Delta T$  the temperature difference between vapor and liquid phase.

### Equilibrium, kinetic and transport parameters

The kinetic parameters of different amines and the equilibrium and transport parameters are tabulated in TABLES 2 and 3.

### Numerical solution

The Eqs. (15)-(22) and Eqs. (30) and (31) form a set of nine differential equations which are solved numerically using an iterative approach and by taking into account the appropriate boundary conditions. First using specification of the reboiler,  $T_R$  and  $Q_R$ , the flow rate and temperature of the gas phase exiting from the reboiler and entering the column at its bottom is determined. While the flow rate, the concentration and the temperature of the liquid phase entering the top of the column are known, to start

TABLE 2 : Rate constants of reaction between amines and  $\text{CO}_2$  where T is liquid temperature (K)

Amine	$k_{AM}$ ( $\text{m}^3 \text{ kmol}^{-1} \text{ h}^{-1}$ )	Ref.
DEA	$6.4 \times 10^8 \exp [14.97(1 - 353/T)]$	[17,28]
MEA	$3.4 \times 10^8 \exp [13.54(1 - 353/T)]$	[17,28]
TEA	$36 \times 10^{(12.72 - 2688/T)}$	[17,28]
MAE	$12 \times 10^8 \exp [13.40(1 - 353/T)]$	[17,28]

the integration procedure, the flow rate, concentration and temperature of the liquid phase at the bottom of the column must to be guessed initially. With these guesses the column equations can be then integrated using the Euler method up to the top of the column. The results obtained from the calculations are, in turn, used for further iteration until a converged solution is obtained. The shooting method was employed in this study to verify the convergence of the solution [33,34].

For this purpose, two values of  $X_b^{(1)}$  and  $X_b^{(2)}$  are assumed for each of the liquid phase properties at the bottom (liquid flow rate, L, liquid temperature,  $T_L$ , and liquid mole fractions,  $X_{\text{K}_2\text{CO}_3}$ ,  $X_{\text{KHCO}_3}$ ,  $X_{\text{H}_2\text{O}}$ ,  $X_{\text{DEA}}$  and  $X_{\text{KVO}_3}$ ). The corresponding calculated values at the top of the column,  $X_t^{(1)}$  and  $X_t^{(2)}$ , are used to calculate the difference functions,  $X_t - X_t^{(1)}$  and  $X_t - X_t^{(2)}$  (where  $X_t$  is the observed liquid property at the top). The points A and B are plotted at  $(X_b^{(2)}, X_t - X_t^{(1)})$  and  $(X_b^{(2)}, X_t - X_t^{(2)})$  on a xy plane. Then the line AB is extended to intersect with the x axis at C, which provides the next guess for  $X_b$ , say  $X_b^{(3)}$  [34] calculated using the following equation:

$$X_b^{(3)} = \frac{X_b^{(2)} - X_b^{(1)}}{X_t^{(1)} - X_t^{(2)}} (X_t^{(1)} - X_t) + X_b^{(1)} \quad (40)$$

A computer program has been written in Fortran language using the above procedure. A step size of 1/100 of the packed height was found to be adequate to achieve a converged solution with a reasonable level of accuracy.

### Model validation

A verification of the model was carried out by comparison with the operating data of an industrial hot carbonate regeneration from Shiraz Petrochemical Complex [18] (see TABLE 1). The predicted results and actual data are presented in TABLE 4. Overall, for all the cases studied a satisfactory agree-

ment was achieved.

## RESULTS AND DISCUSSION

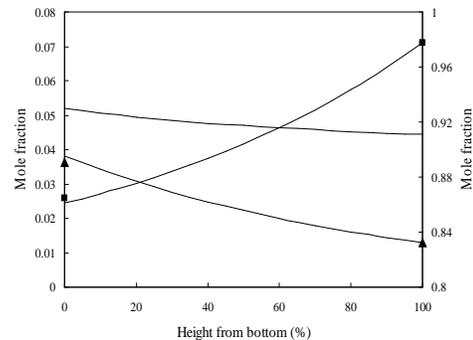
The performance of the carbon dioxide desorption was investigated by conducting desorption simulations under the design and operating conditions summarized in TABLES 1 and 4. The simulation results were plotted and the effects of different parameters on the desorption performance were examined.

The concentration of components in the liquid phase changes along the stripper column due to the desorption of  $\text{CO}_2$  from solution. The mole fraction profiles for  $\text{K}_2\text{CO}_3$ ,  $\text{KHCO}_3$  and  $\text{H}_2\text{O}$  in liquid phase are represented in figure 3. Since  $\text{KHCO}_3$  is consumed due to reaction, the concentration of  $\text{KHCO}_3$  in the solution decreases as it moves down the column. Water concentration profile is affected by water vapor condensation and water generation by the liquid phase reaction. According to these effects, the concentration of water increases along the column from top to bottom. Since  $\text{K}_2\text{CO}_3$  is a reaction product its concentration increases as the liquid moves down the column.

The temperature profiles have been calculated by using the model along the packed bed as shown in Figure 4. The gas temperature decreases as it moves

**TABLE 4 : Comparison of calculated results with the observed plant data<sup>[18]</sup> under the specification indicated in TABLE 1.**

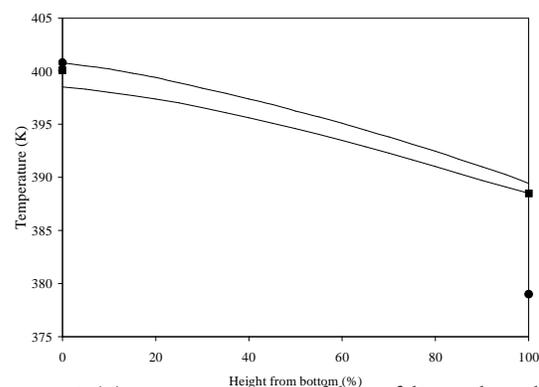
Parameters	Inlet	Outlet observed	Calculated	Error %
Liquid emperature (K):	388	401	398.5	0.62
Liquid flow rate (kmol/h):	63660	61677	61179	0.81
Liquid composition (mole fraction):				
$\text{K}_2\text{CO}_3$	0.01260	0.03663	0.03812	-4.06
$\text{KHCO}_3$	0.07110	0.02527	0.02456	2.81
WATER	0.90766	0.9294	0.9277	0.18
DEA	0.00717	0.00722	0.00746	-3.32
$\text{KVO}_3$ (anti-corrosion)	0.00144	0.00145	0.00149	-2.76
Gas temperature(K)	401	379	391.82	-3.38
Gas flow rate (kmol/h)	3990	3950	4210	-6.6
Gas composition (mole fraction):				
$\text{CO}_2$	0.0	0.3645	0.3491	4.22
$\text{H}_2\text{O}$	1.0	0.6355	0.6509	-2.4



**Figure 3: Concentration profile of various components in liquid phase along the packed bed**

up the stripper since heat is being transferred to the liquid phase due to condensation of water vapor and the temperature difference. The absorption of heat by chemical reactions in the liquid phase is negligible in comparison with the sum of the heat which is being transferred to the liquid phase due to the condensation and temperature difference so that the liquid temperature increases as it moves down the stripper.

The absorbed  $\text{CO}_2$  in the buffer solution of carbonate-bicarbonate is stored in the ionic form  $\text{HCO}_3^-$ . The concentration of bicarbonate ion decreases as liquid comes down from up to bottom of column due to the stripping of  $\text{CO}_2$ . Therefore, according to definition of  $\alpha$ , carbonation ratio in the liquid phase along the length of column is decreased from top to bottom as shown in figure 5a, while concentration of  $[\text{CO}_3^{2-}]$  due to chemical reaction is increased as shown in figure 5b. Concentration of  $\text{OH}^-$  depends on the ratio of the concentration of carbonate to bicarbonate ion so that its concentration is increased as liquid moves down the column.



**Figure 4. Temperature profiles of liquid and gas phase along the packed bed height**

## Full Paper

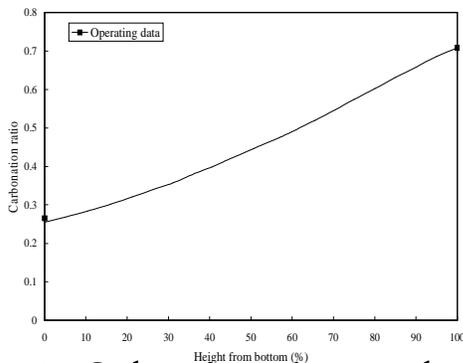


Figure 5a : Carbonation ratio versus the packed bed height

Since in a carbonate-bicarbonate mixture,  $\text{HCO}_3^-$  is consumed while  $[\text{CO}_3^{2-}]$  is generated, the concentration of free  $\text{CO}_2$ , which would be in equilibrium with local concentration of  $\text{HCO}_3^-$  and  $[\text{CO}_3^{2-}]$  are decreased as liquid moves down as shown in figure 5b.

In figure 6, effect of the inlet liquid temperature on separation efficiency of the stripper is studied while separation efficiency is defined as<sup>[20,23]</sup>:

$$\eta_{\text{reg}} = \frac{Q_{\text{CO}_2}}{m_s} \quad (41)$$

In the above equation  $Q_{\text{CO}_2}$  is volumes of  $\text{CO}_2$  ( $\text{m}^3/\text{h}$ ) removed, and  $m_s$  the mass flow rate of steam ( $\text{kg}/\text{h}$ ) used in the reboiler. In sensitivity analysis of Figure 6 the stripper is operated so that a constant lean loading is provided.

This figure clearly shows the higher mass-transfer performance at higher inlet temperatures, which can be presented by increasing the equilibrium vapor pressure of  $\text{CO}_2$  over the portion of solution last contacted by the gas. It is clear that at lower temperatures, the stripping curve has a horizontal

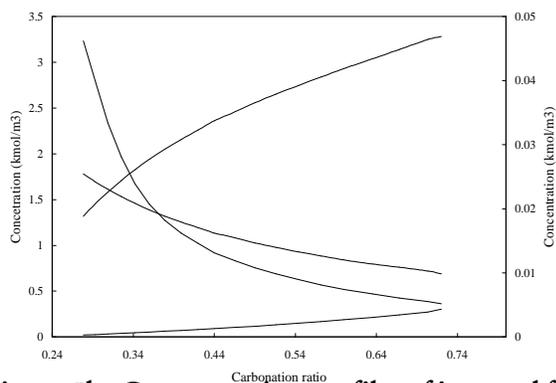


Figure 5b : Concentration profiles of ions and free  $\text{CO}_2$  versus carbonation ratio

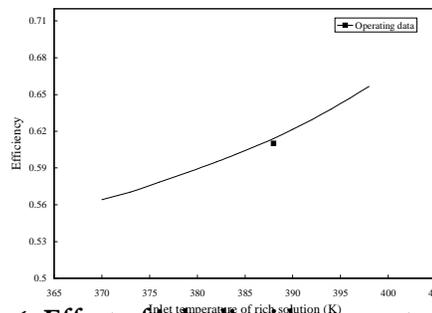


Figure 6: Effect of inlet liquid temperature on regeneration efficiency

asymptote, so a large increase in the inlet liquid temperature is required to obtain a small increase in efficiency. Hence, beside the influence of the equilibrium vapor pressure of  $\text{CO}_2$ , the steam consumption rate ( $m_s$ ), which indirectly depends on the liquid temperature plays an important role on the stripping performance.

A change in the promoter concentration obviously has an impact on the desorption performance while the stripper is operated to provide a constant lean loading. According to figure 7, an increase in the amine concentration induces a higher  $\text{CO}_2$  stripping. The possible explanation for this behavior is that increasing the amine concentration reflects the higher enhancement factor in the liquid phase, which is directly proportional to the overall KL in the case of liquid phase controlled mass transfer.

Promoter type is considered as another essential factor affecting the efficiency of  $\text{CO}_2$  desorption process. According to figure 8 the role of four types of amines were compared for their effectiveness in carbon dioxide stripping at identical operating conditions. These were DEA, MEA, TEA and MAE. As shown in figure 8, MAE provides the highest mass

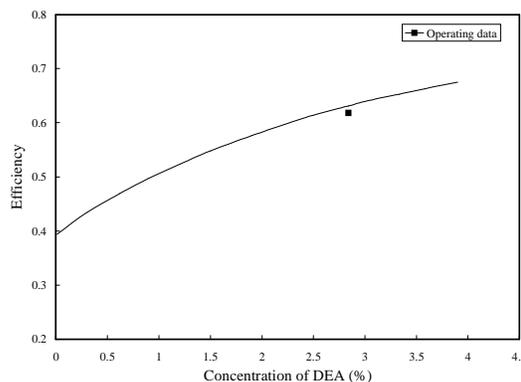


Figure 7: Effect of DEA concentration on regeneration efficiency

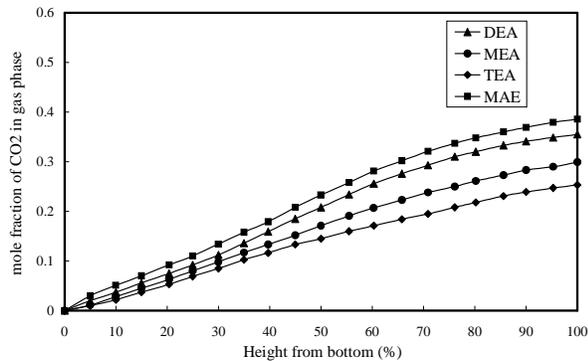


Figure 8 : Effect of amine type on mole fraction of  $\text{CO}_2$  along the column height

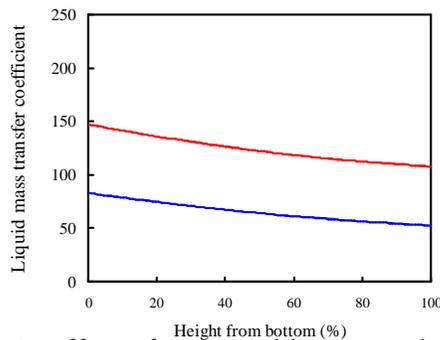


Figure 9: Effect of amine addition on the liquid phase mass transfer coefficient along the column

transfer performance when compared with MEA, TEA and DEA. The difference between the regeneration efficiency by three of the amines is preliminary influenced by the second order rate constant,  $k_{AM}$  as indicated in TABLE 2. According to this TABLE, the value of  $k_{AM}$  for the  $\text{CO}_2$  - MAE system is greater than that of  $\text{CO}_2$  - MAE,  $\text{CO}_2$  - TEA and  $\text{CO}_2$  - DEA, thus leading to a higher enhancement factor and regeneration efficiency.

The role of amine in the mass transfer performance is shown in figure 9. As can be seen, addition of amine to the liquid phase induces liquid phase mass transfer coefficient ( $k_L^E$ ). The difference between the liquid phase mass transfer coefficients for amine and amine-free solution is preliminary influenced by the second-order rate constant,  $k_{AM}$ , as indicated by Eq. (12). An increase in  $k_{AM}$  reflects the higher enhancement factor in the liquid phase (Eq. (35)) which is directly proportional to the liquid phase mass transfer coefficient as shown in Eq. (34).

## CONCLUSION

A numerical model was developed and validated for simulation of carbon dioxide desorption from promoted hot potassium carbonate in industrial-scale strippers. The proposed model accurately predicted the stripper performance when the predictions were compared with observed data. The effect of three parameters on stripper performance was investigated; inlet liquid temperature, promoter concentration and promoter type. The inlet liquid temperature was found to possess two important effects on the general behavior of the stripper. Firstly, it influences the mass transfer process and secondly the steam consumption rate of reboiler. In the stripper which is controlled by the liquid side mass transfer, the increase of  $E$  with increasing the weight percent of amine in the solution, demonstrates that the resistance in the liquid phase is decreased as amine is added to the solution. The use of other amines is an efficient way to enhance the regeneration efficiency of desorption process which has been discussed in this work. The model provides a procedure to investigate the effect of new promoters on the  $\text{CO}_2$  desorption.

## ACKNOWLEDGEMENTS

The authors would like to thank Shiraz Petrochemical Complex for providing valuable data. The financial support provided by the University of Newcastle, Australia, is greatly appreciated. Also the financial support of this work by Shiraz University under grant of research project 82-EN-1605-C242 is gratefully acknowledged.

## Nomenclature

$\alpha$	specific surface area ( $\text{m}^2 \text{m}^{-3}$ )
$C_k$	concentration of $k^{\text{th}}$ component ( $\text{kmol m}^{-3}$ )
$C_{k_e}$	equilibrium concentration of $k^{\text{th}}$ component in the bulk of liquid ( $\text{kmol m}^{-3}$ )
$C_{k_i}$	concentration of $k^{\text{th}}$ component at interface ( $\text{kmol m}^{-3}$ )
$C_{p_g}$	average molar specific heat of gas ( $\text{kJ kmol}^{-1} \text{K}^{-1}$ )
$C_{p_k}$	average specific heat of $k^{\text{th}}$ component ( $\text{kJ kmol}^{-1} \text{K}^{-1}$ )
$C_{p_L}$	molar specific heat of liquid ( $\text{kJ kmol}^{-1} \text{K}^{-1}$ )
$C_{pL}$	specific heat of liquid ( $\text{kJ kg}^{-1} \text{K}^{-1}$ )
$D_{\text{LCO}_2}$	diffusivity of $\text{CO}_2$ in $\text{K}_2\text{CO}_3$ solution ( $\text{m}^2 \text{m}^{-1}$ )
$D_{g\text{CO}_2}$	diffusivity of $\text{CO}_2$ in gas ( $\text{m}^2 \text{h}^{-1}$ )
$d_p$	packing nominal size (m)
$E$	enhancement factor
$G$	molar velocity of gas ( $\text{kmol m}^{-2} \text{h}^{-1}$ )

TABLE 3 : Equilibrium, kinetics and transport parameters

parameter	expression	source
$\alpha$	$\alpha = \frac{[K^+] - 2[CO_3^{2-}]}{[K^+]} = \frac{[HCO_3^-]}{[K^+]}$	[16]
$P_{H_2O_i}$	$\log P_{H_2O_i} = -(L' / 2.303R)((1/T) - 2.45 \times 10^{-3}) - 1.1672 + C$ ; $L' = 40983.6$	[34]
$C$	$C = 1.2014 + (0.2857 / x_c) - (0.0537 / x_c^2)$	[34]
$x_c$	$x_c = \frac{0.691(\% KHCO_3)}{\% K_2CO_3 + 0.691(\% KHCO_3)}$	[34]
$P_{CO_{2e}}$	$P_{CO_{2e}} = 2 \frac{K_2[K^+]}{K_1 H} \frac{\alpha^2}{1 - \alpha}$	[16]
$K_5$	$\log(K_5) = -(3404.7 / T) + 14.843 - 0.03279T$	[16]
$K_6$	$\log(K_6) = -(2902.4 / T) + 6.498 - 0.0238T$	[16]
$H$	$\log(H / H_w) = -K_s I$ ; $K_s = 0.06$ , $I = 6.2$	[16]
$H_w$	$\log H_w = (1140 / T) - 5.30$	[16]
$k_{OH}$	$\log(k_{OH}) = 13.635 - (2895 / T) + 0.08I$	[35]
$k_{gk}$	$\frac{k_{gk} RT}{aD_{gk}} = 5.32 \left( \frac{\hat{G}}{a\mu_g} \right)^{0.7} \left( \frac{\mu_g}{\rho_g D_{gk}} \right)^{1/3} (ad_p)^{-2.0}$	[23]
$k_L$	$k_L \left( \frac{\mu_1^2}{\rho_1^2 g} \right)^{1/3} / D_{CO_2} = 0.015 \left( \frac{\hat{L}}{a\mu_1} \right) \left( \frac{\mu_1}{\rho_1 D_{CO_2}} \right)^{1/3}$	[36]
$D_{CO_2}$	$\log D_{CO_2} = -3.0188 - \frac{586.9729}{T} - 0.4437$	[15]
$h_g$	$h_g = \sum_k y_k h_{gk}$	[37]
$h_{gk}$	$h_{gk} = k_{yk} C_{pk} (Le)^{2/3}$	[37]
$C'_P$	$C'_P = 4.1774 - 0.0382\omega - 0.4445 \times 10^{-3} \omega^2 + 1.2798 \times 10^{-5} \omega^3$	[20]
$\Delta H_{CO_2}$	$\Delta H_{CO_2} = 27228.2 + 81.37\omega + 5.32\omega^2 - 0.1313\omega^3 + 1.654 \times 10^{-3} \omega^4$	[38]
$\omega$	$\omega = \frac{\% K_2CO_3 + 0.691(\% KHCO_3)}{\% K_2CO_3 + 0.781(\% KHCO_3) + \% H_2O}$	[22]

$\hat{G}$	mass velocity of inert gas ( $kg\ m^{-2}\ h^{-1}$ )	$k_{OH}$	backward rate constant of reaction (3) ( $s^{-1}$ )
$G_R$	molar velocity of vapor leaves the reboiler ( $kmol\ h^{-1}$ )	$K_g$	overall mass transfer coefficient ( $kmol^{-1}\ m^{-2}\ atm^{-1}$ )
$H$	solubility of carbon dioxide in solution ( $kmol\ atm^{-1}\ m^{-3}$ )	$K_y$	Gas side mass transfer coefficient ( $kmol\ h^{-1}\ m^{-2}$ )
$H_{VAPOR}$	enthalpy of superheated steam ( $kJ\ kmol^{-1}$ )	$k_L$	liquid side mass transfer coefficient ( $mh^{-1}$ )
$h$	heat transfer coefficient in gas phase ( $kJ\ m^{-2}\ h^{-1}\ K^{-1}$ )	$K_5$	first ionization constant for carbonic acid ( $kmol\ m^{-3}$ )
$h_c$	condensing heat transfer coefficient ( $kJ\ m^{-2}\ h^{-1}\ K^{-1}$ )	$K_6$	second ionization constant for carbonic acid ( $kmol\ m^{-3}$ )
$\Delta H_{CO_2}$	heat of reaction and absorption of $CO_2$ ( $kJ\ kmol^{-1}$ )	$L$	molar velocity of liquid ( $kmol\ m^{-2}\ h^{-1}$ )
$\Delta H_{H_2O}$	heat of vaporization of water ( $kJ\ kmol^{-1}$ )	$\hat{L}$	liquid mass flow rate ( $kg\ h^{-1}$ )
$I$	ionic strength of solution ( $kJ\ ion\ m^{-3}$ )	$Le$	Lewis number
$k$	pseudo first order rate constant ( $h^{-1}$ )	$N_k$	mass transfer flux of kth component ( $kmol\ m^{-2}\ h^{-1}$ )
$k_{AM}$	second order rate constant of amine ( $m\ kmol^{-1}\ h^{-1}$ )	$P_k$	partial pressure of kth component in gas phase (atm)
$k_{OH}$	forward rate constant of reaction (3) ( $m^{-3}\ kmol^{-1}\ s^{-1}$ )	$N_{ke}$	equilibrium vapor pressure of kth component in gas phase (atm)
$k_g$	Gas side mass transfer coefficient ( $kmol\ h^{-1}\ m^{-2}\ atm^{-1}$ )		

$P_{K_i}$	partial pressure of kth component in in the liquid-gas interface (atm)
pr	Prantl number
$Q_R$	reboiler heat load ( $\text{kJ h}^{-1}$ )
R	universal gas constant ( $\text{m}^3 \text{ atm kmol}^{-1} \text{ K}^{-3}$ )
Re	Reynolds number
S	cross sectional area of column ( $\text{m}^2$ )
$T_g$	gas temperature (K)
$T_L$	liquid temperature (K)
t	liquid temperature (K)
$W_v$	mass velocity of vapor ( $\text{kg h}^{-1}$ )
$X_k$	mole fraction of kth component in the liquid phase
$Y_k$	mole fraction of kth component in the gas phase

## Greek symbols

$\alpha$	carbonation ratio
$\mu_g$	gas phase viscosity ( $\text{kg m}^{-1} \text{ h}^{-1}$ )
$\mu_v$	vapor phase viscosity ( $\text{kg m}^{-1} \text{ h}^{-1}$ )
$\mu_L$	liquid phase viscosity ( $\text{kg m}^{-1} \text{ h}^{-1}$ )
$\rho$	gas phase density ( $\text{kg m}^{-3}$ )
$\rho_L$	liquid phase density ( $\text{kg m}^{-3}$ )
$\omega$	total equivalent weight percent of $\text{K}_2\text{CO}_3$

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