

## Alternate Proof For Expression of Most Probable Speed of Gas

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### Introduction

Most probable speed is the speed most likely possessed by any gas (of the same mass) in the system. It can be derived using Maxwell-Boltzmann distribution function [1] for ideal gases. I will provide an alternate derivation by using the definition, gas laws and kinetic theory of gases.

### Preliminaries

Boyle's law: The absolute pressure exerted by given mass of an ideal gas is inversely proportional to the volume it occupies if the temperature and amount of gas remains unchanged with in a closed system [2]. In an elastic collision the total kinetic energy of the system is constant [3].

### Main Result

The most probable speed of the gas is given by,

$$V_p = \sqrt{\frac{2RT}{M}}$$

where  $V_p$  is the most probable speed of the gas, R is the universal gas constant, T is the absolute temperature of the system and M is the molecular mass of the gas. Proof: Consider a given amount of ideal gas in a closed system at constant temperature. By Boyle's

$$pv = \text{constant}$$

and for a given amount of gas and at constant temperature by assumptions of kinetic theory of gases

$$\frac{1}{2}(mV_1^2 + mV_2^2 + \dots + mV_N^2) = \text{constant}$$

since equation one and two are constant for same parameters and dimensionally energies, we can equate them

$$\frac{1}{2}(mV_1^2 + mV_2^2 + \dots + mV_N^2) = pv$$

$$\frac{m}{2}(V_1^2 + V_2^2 + \dots + V_N^2) = pv$$

,using the definition of most probable speed, let's say all of the molecules are moving with  $V_p$

$$\frac{m}{2}(V_p^2 + V_p^2 + \dots + V_p^2) = pv$$

$$\frac{Nm}{2} V_p^2 = pV$$

,where N is the total number of molecules and Nm is the mass of the gas

$$\frac{NmV_p^2}{2V} = p$$

But,

$$\frac{Nm}{V} = d$$

,d=density of the gas

$$\frac{dV_p^2}{2} = p$$

$$p = \frac{dRT}{M}$$

$$dV_p^2 = \frac{2dRT}{M}$$

$$V_p^2 = \frac{2RT}{M}$$

$$V_p = \sqrt{\frac{2RT}{M}}$$

hence proved.

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### References

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2. Levine, Ira N. "Physical Chemistry" University of Brooklyn: McGraw-Hill, 1978.
3. Craver, William E. [Elastic collisions](#). 2013.