



## **THE CALCULATION OF ANISOTROPIC PROPERTIES ON THE BASE OF ENGINEERING STRUCTURES**

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### **ABSTRACT**

We consider the definition of the kernel function and the effect of a transversely isotropic half-space. Expressions are derived deflections and internal forces in an infinite base plate in accordance with their recesses in the mountain range, as well as the influence of anisotropy on the base distribution of deflections and internal forces.

**Key words:** Anisotropic properties, Engineering structures and kernel.

### **INTRODUCTION**

Improved economic performance in construction is directly related to the use of more advanced designs, including a large place occupied by the deformable structure basis. These are the foundations and structures erected in areas with rugged. Cost bases and foundations of modern engineering structures in the piedmont areas of 15-20 percent of the value of all construction<sup>1-3</sup>. Along with the knowledge of the stress-strain state of the structures and foundations of buildings, it is extremely important to study the soil forming the base, the properties of which are included in the design parameters of load-bearing structures. It is particularly important to determine the strength of the subgrade shear and

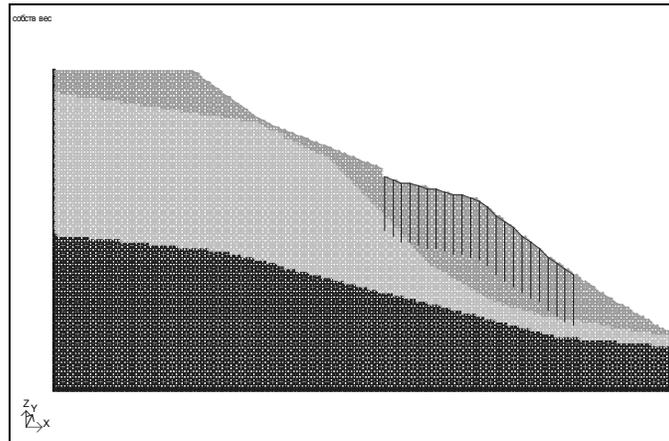
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fracture pressure. The accuracy of the data will be improved if we consider the anisotropic deformation and strength properties of the subgrade, the orientation of the plane of isotropy with respect to the surface of the soil mass and the distribution of stresses in the ground bearing foundations of buildings on the anisotropic base<sup>4-6</sup>.

Geometric nature and the degree of anisotropy of rocks depends on the mineralogical composition, structure, texture, but most of these features are related to the conditions of formation bedding, followed by metamorphism, and the advent of fracture<sup>2,7,8</sup>.

Variety of properties of soil bases, depending not only on the conditions of their natural occurrence, but also on the stress-strain state, humidity, and temperature, etc., cannot be described adequately and in detail with the help of simple circuits. The problem arises of creating more complex models bases that do not contradict the basic positions of soil mechanics and structural mechanics. The question of a plausible scheme of the base, the analysis of the various competing models and the choice of an appropriate computational model of the base are very critical part of the design. Clarification of the elastic module of the base and to determine their parameters experimentally increase the reliability of research results. Development of more computerized calculation methods will reduce the development time of these structures and thus reduce the share of design work. All this leads to a more economical and, therefore, decreases the labor and materials for the construction of structures. To identify features of anisotropic basis is necessary to conduct experimental research (Fig. 1)<sup>9,10</sup>.



**Fig. 1: General view of the design scheme of the slope - the ski base jumping in Almaty**

In general, the rock mass has the property of elastic anisotropy, which is primarily a consequence of the manifestation of layering and fracturing rock strata. For the first time the feasibility of accounting elastic anisotropy of rocks contains S. G. Lehnitskim consider only the horizontal layering of the array of simulated transversely elastic body, the plane of isotropy coincides with the bedding plane layers<sup>12</sup>.

Anisotropic model finely layered array ramp isotropy, first used by Erzhanovym et al.<sup>5</sup>

Experimental data on soil bases in the construction of the ski jump in Almaty showed that the investigated rock massif has transversalno-isotropic properties: modulus of elasticity  $E_2$  along the bedding layers twice the elastic modulus  $E_1$  in the direction perpendicular to the plane of isotropy, i.e.  $E_1 > E_2$ , ( $E_1 = 2E_2$ ). Therefore, to calculate the support structures springboard, was considered a model of subgrade, taking into account the anisotropic properties of the soil<sup>11,12</sup>.

As it is well known, the properties of the base characterized by the influence function  $c(\alpha, \beta)$ , which the form depends on the model adopted base. For some reason kind of function  $(\alpha, \beta)$  presented in the works of Korenev. Before proceeding to the study of the stress-strain state of structures and foundations of buildings, lying on a linearly deformable uniform basis, first consider an important auxiliary problem of the relationship between the vertical forces acting on the basis and foundation deflections<sup>13,14</sup>.

We will consider the kernel, which can be represented graphically in the form of a surface of revolution, i.e., kernels of the form –

$$K(x - \xi, y - \eta) = K\left(\sqrt{(x - \xi)^2 + \mu(y - \eta)^2}\right) \quad \dots(1)$$

Where  $\mu$  - is a constant

The corresponding model base may be of value in the anisotropy in the xy-plane, as well as in dealing with dynamic problems. For the design of structures and foundations of buildings on elastic anisotropic basis, it is necessary to determine the dependence of the vertical displacements of the ground surface from the action on the surface of the concentrated force.

As a model of anisotropic foundation is transversely-isotropic half-space having the following physical and mechanical properties:  $E_z = E_1$  – modulus of longitudinal elasticity

in the vertical direction;  $E_r = E_2$  – modulus of longitudinal elasticity in the horizontal direction (in-plane isotropic);  $\nu_1$  – Poisson's ratio characterizing transverse contraction in the plane of the anisotropy in tension in the direction perpendicular to it;  $\nu_2 = \nu$  – Poisson's ratio corresponding to the stretching in the plane anisotropy and characterizing the transverse compression in the plane;  $G, G_2$  – shear module, respectively, to the plane of isotropy and perpendicular to it. The modulus  $G_2$  is received the lowest for any ratio of the module of elasticity. In the presence of the specific values of the shear module determined experimentally for real soils may be included in the formulas obtained. Specifications and strain coefficients on Bekhterev can be expressed as follows:

$$\begin{aligned} a_{11} &= \frac{1}{E_r}, a_{12} = -\frac{\nu}{E_r}, a_{33} = \frac{1}{E_z}; \\ a_{13} &= \frac{\nu_1}{E_z}, a_{44} = \frac{1}{G_R}, 2(a_{11} - a_{12}) = \frac{2(1+\nu)}{E_r} = \frac{1}{G_K} \end{aligned} \quad \dots(2)$$

Vertical movement of the direction of the x-axis under the action of axisymmetric forces expressed in terms of the stress function  $\varphi$ <sup>12</sup>:

$$w = \alpha \left( \frac{\partial^2 \varphi}{\partial r^2} + \frac{1}{r} \frac{\partial \varphi}{\partial r} + \beta \frac{\partial^2 \varphi}{\partial z^2} \right) \quad \dots(3)$$

где  $\alpha = \frac{1}{A_{44}}; \beta = \frac{A_{44}}{A_{11}}; A_{ij}$  – elastic module;

$$A_{11} = \frac{a_{11}a_{33} - a_{13}}{(a_{11} - a_{12})m}; A_{44} = \frac{1}{a_{44}}; m = (a_{11} - a_{12})a_{13} - 2a_{13}^2$$

Function  $\varphi$  must satisfy the differential equation:

$$\nabla_1 \nabla_2 \varphi = 0 \quad \dots(4)$$

Where  $\Delta_i = \frac{\partial^2}{\partial r^2} + \frac{1}{r} \cdot \frac{\partial}{\partial r} + \frac{1}{s_i^2} \cdot \frac{\partial^2}{\partial z^2}, \quad (i = 1, 2).$

Function  $\varphi$  is defined as follows:

$$\varphi = \int_0^{\infty} (C e^{-s_1 \lambda z} + D e^{-s_2 \lambda z}) J_0(\lambda r) d\lambda \quad \dots(5)$$

Where  $\lambda$  - parameter integration;

$S_1, S_2$ - roots of the characteristic equation:

$$s_1 = \frac{\sqrt{a+c} + \sqrt{(a+c)^2 - 4d}}{2d}; \quad s_2 = \frac{\sqrt{a+c} - \sqrt{(a+c)^2 - 4d}}{2d};$$

$$C = -\frac{\Psi(\lambda)}{\lambda^2} \cdot \frac{(1 - as_2^3 \sqrt{d})}{(s_1 - s_2)(ac - d)}; \quad D = -\frac{\Psi(\lambda)}{\lambda^2} \cdot \frac{(1 - as_1^3 \sqrt{d})}{(s_1 - s_2)(ac - d)};$$

$$a = -\frac{a_{13}(a_{11} - a_{12})}{a_{11}a_{33} - a_{13}^2}; \quad c = -\frac{a_{13}(a_{11} - a_{12}) + a_{11}a_{44}}{a_{11}a_{33} - a_{13}^2}; \quad d = \frac{a_{13}^2 - a_{12}^2}{a_{11}a_{33} - a_{13}^2}$$

Function  $\psi(\lambda)$ , included in the expressions for C and D, corresponding to a given load q and is determined by the Hankel Transform:

$$q(\lambda) = \int_0^{\infty} q(\xi) \xi \cdot J_0(\lambda \xi) d\xi \quad \dots(6)$$

Substituting (5) into (4) and solving the equation we obtain the formula for finding the displacement:

$$w = \frac{P\alpha}{2\pi(s_1 - s_2)} \left( \frac{\xi_1}{\sqrt{r^2 + s_2^2 z^2}} - \frac{\xi_2}{\sqrt{r^2 + s_1^2 z^2}} \right) \quad \dots(7)$$

Moving surface transversely isotropic half-space we obtain from (7) at  $z = 0$ :<sup>15</sup>

$$w_{z=0} = \frac{P\alpha(s_1 + s_2)(a - \beta)\sqrt{d}}{2\pi(ac - d)r} \quad \dots(8)$$

Kernel for transversely isotropic elastic half-space will get by putting in (7)  $P = 1$ :

$$K(r) = \frac{\alpha(s_1 + s_2)(a - \beta)\sqrt{d}}{2\pi(ac - d)r} \quad \dots(9)$$

Now, substituting (9) into the expression for the function  $c(\lambda)$ , characterizing the model base, we obtain:

$$c(\lambda) = \frac{\alpha(s_1 + s_2)(a - \beta)\sqrt{d}}{(ac - d)} \cdot \frac{1}{\lambda} \quad \dots(10)$$

Denote

$$k_{TP} = \frac{(ac - d)}{\alpha(s_1 + s_2)(a - \beta)\sqrt{d}} \quad \dots(11)$$

Then 
$$c(\lambda) = \frac{1}{k_{TP}\lambda} \quad \dots(12)$$

For the kernel transversely isotropic half-space ratio  $k_{TP}$  is –

$$k_{TP} = \frac{ac - d}{\alpha(s_1 + s_2)(a - \beta)\sqrt{d}} = \frac{E_z}{2\bar{w}_{z=0}} \quad \dots(13)$$

The expression obtained kernel transversely isotropic half-space with the horizontal plane of isotropy differs from the corresponding core isotropic half-space ratio  $\bar{w}_{z=0}$ , which takes into account the anisotropy of the base according to the relationship  $E_z/E_r = k_{TP}$ , values  $\nu_1$  and  $\nu_2$ . The analytical expression of deflections and internal forces in the base plate, given its penetration in the subsurface array can solve a number of problems in an analytical form, for infinite and finite for foundation slabs, using the methods-time work in the<sup>16</sup>.

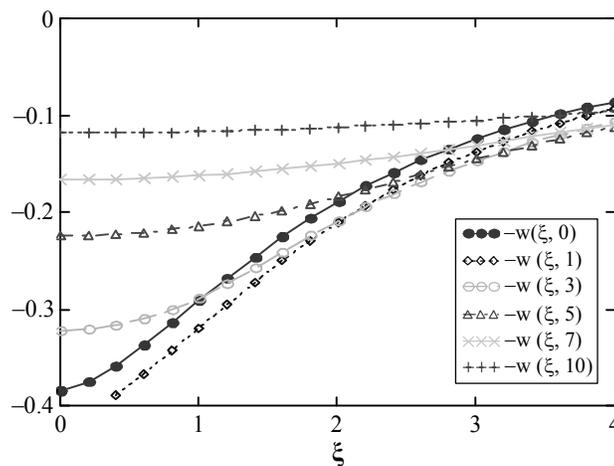
Calculation plates lying on the surface of the anisotropic base, i.e. at  $z = 0$ , are considered in<sup>17,18</sup>. Study the distribution patterns of movement within and on the boundary of a deformable half-space under the action of a force applied to the boundary plane, carried out by Zaletov and Hrapilova<sup>19</sup>.

For example, consider the case of anisotropy  $k_E = 5$ . Figures 1-5 show the diagrams deflections; radial, tangential bending moments and shear forces in the endless base plate loaded by a concentrated force  $P = 1$  for values

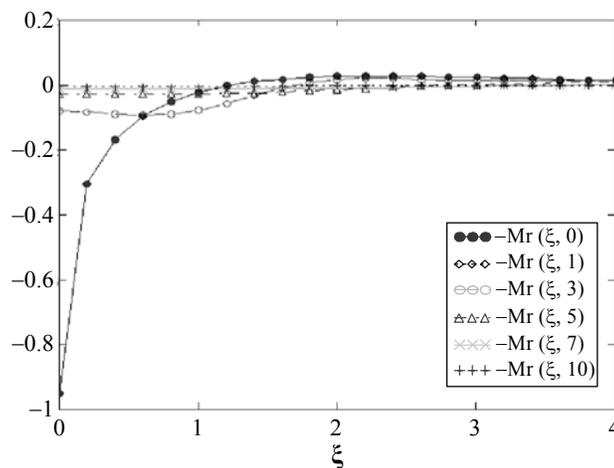
$$z = 0, 2, 3, 5, 10 \text{ and } E_z = 50 \text{ MPa; } M_r = 10 \text{ MPa.}$$

The results show a significant influence of anisotropy on the base of the distribution of values of deflections and internal efforts to change the depth of the

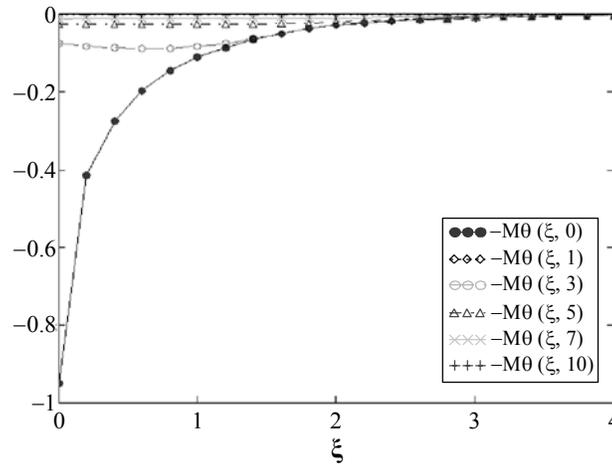
foundation plates. For example, the values of the deflection plates at  $z = 0$  for the isotropic case is  $-w = 0.385$ , and when  $z = 10$  for the anisotropic case, respectively  $-w = 0.118$ , i.e. value of the deflection is more than 3.3 times the value of the deflection plates on the basis of an isotropic with the same penetration. A similar pattern is observed for the internal forces<sup>20,21</sup>.



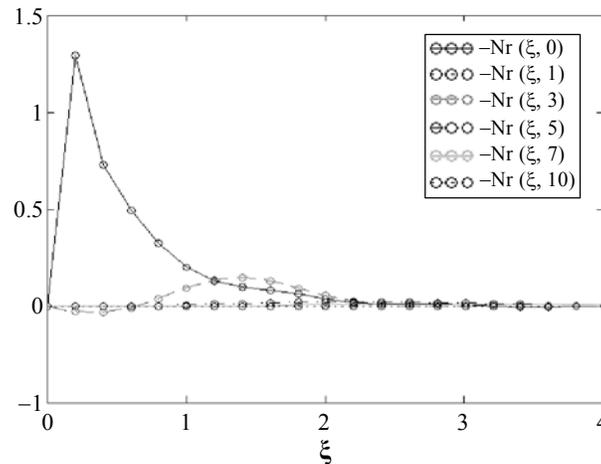
**Fig. 2:** The diagram of figure 1 in an endless deflection plate at  $k_E = 5$  is loaded by a concentrated force  $P = 1$  is given recess at  $z = 0, 2, 3, 5, 7, 10$



**Fig. 3:** Radial bending moments in an infinite plate with  $k_E = 5$ , loaded by a concentrated force  $P = 1$  when the light of improved  $z = 0, 2, 3, 5, 7, 10$



**Fig. 4:** The diagram of the tangential bends moments in an infinite plate with  $k_E = 5$ , loaded by a concentrated force  $P = 1$  with the deepening at  $z = 0, 2, 3, 5, 7, 10$



**Fig. 5:** The diagram of shear forces in an infinite plate with  $k_E = 5$ , loaded by a concentrated force  $P = 1$  with the deepening at  $z = 0, 2, 3, 5, 7, 10$

### CONCLUSION

The results obtained in this paper can also be used as a criterion to assess the validity of the results obtained in the numerical studies. Based on these dependencies identified the stress-strain state of the soil, which is based on the foundations of the ski jump in Almaty.

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